

# AN EXERCISE ON THE FUTURE HEALTH DEVELOPMENTS IN GREECE

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## Abstract

After developing a stochastic analysis for the estimation of healthy life expectancy of human populations, a demonstration of the application of a new and simplified method to assess the future health trends of a population will take place in this paper. Data comes from the population projections of Greece, carried out a few years ago, including the estimated mortality forecasts. In the form of complete life tables, these forecasts will be used to estimate healthy life expectancy until the year 2050, which will depend on the different scenarios created during the projections' procedure. The results of the analysis indicate the validity and applicability of the method used whenever lifetable data is available.

**Key words:** healthy life expectancy, population projections, mortality forecasts, Greece

**JEL Code:** I1, J10, J26

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## Introduction

During the last decades, many scholars tried to estimate the health level of a population, following WHO's (1948) definition of health, which is "*a state of complete, physical, mental and social wellbeing*". Such measures were the "*index of health*" (Chiang, 1965), the "*effective life years*" (the years a person can fulfil its role in the society; Sanders, 1964), the "*expectation of life free of disability*" (Sullivan, 1966, 1971) and others.

In more recent years, more sophisticated procedures were developed both by the WHO, aiming to calculate "*healthy life expectancy*", i.e., the difference between life expectancy at birth and the healthy years lost because of diseases (Vos et al., 2017), and by Eurostat (n.d.); based on Sullivan's method 1966, 1971). In the latter, health is defined by the absence of functionality/disability limitations. However, both methods require knowledge of the prevalence of diseases or disabilities in a population, which is not always available. For example, such data are absent for historical populations. Moreover, if one wishes to estimate health levels in the future, several problems denoting the inefficiency of these methods for such purposes will emerge.

Instead, another method originating from the stochastic theory (see Jansen and Skiadas, 1995) is fully functional and effective, based on lifetable data alone. Recently, Skiadas and Skiadas (2020) simplified this approach and found that the Weibull model and the cumulative hazard *"can express the additive process regarding what disabilities and diseases affect the human organism during the lifespan leading to healthy life years lost"*. Thus, they derived a general model of survival-mortality, estimating a parameter related to the healthy years lost (consequently to an estimation of healthy life expectancy) and leading to the Weibull model and its shape parameter as a particular case (see the Skiadas and Skiadas, 2020 for the mathematical formulas and calculations).

In that way, the scope of this paper is to demonstrate the application of this method with mortality forecast data, an essential element of populations' projection. Greece will be used as a case study.

## **1 Population projections and mortality forecast.**

The population projections of Greece were conducted in 2016, aiming to estimate the population size and structure of the country until 2050 (Kotzamanis et al., 2016). By that time, the number of births and fertility was decreased, while the number of deaths increased due to the population ageing, and the negative balance of the vital rates. The negative immigration balance further burdened the Greek population, and the country was going through a severe economic and social crisis.

The base year for these projections was 2014; thus, these projections were carried out several years ago, ignoring any developments that occurred meanwhile (for example, the coronavirus crisis). Therefore, any future estimations of the healthy life expectancy should be treated with caution, while keeping in mind that the main scope of this paper is to demonstrate the application of the Skiadas and Skiadas (2020) method on mortality forecasts.

Considering Greece's economic and social situation in 2016, two paths were created to formulate the scenarios of the future trends of mortality, fertility, and migration, needed for the projections' procedure.

- Path 1: Resilience. Greece will follow an economic and developmental growth course, being part of the eurozone area without further deregulation of the labour market and social spending and welfare reductions. A progressive decrease in unemployment, especially among young people, will occur in the future.

- Path 2: Inequality. The economic crisis continues, exacerbating its adverse social effects and increasing inequalities.

### 1.1 The mortality forecasts

Within these paths 3 mortality forecasts scenarios were created (Tables 1 and 2):

- Scenario 1. Path 1. Progressive and mild reduction in the probabilities of death. "Medium-high" scenario. An increase in life expectancy at the end of the projection period. A deceleration of mortality decrease in the ages <10 and 30-65 years. A continuing decrease of mortality over 65 years. A slight increase of mortality in younger adult males (20-35 years), which will stabilize afterwards. Mortality in females of the same ages will remain almost stable.

**Tab. 1: Probabilities of death forecasts by large age groups. Males.**

|            |       | 2015-2019 | 2020-2024 | 2025-2029 | 2030-2034 | 2035-2039 | 2040-2044 | 2045-2049 |
|------------|-------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Scenario 1 | 1q0   | 3.8       | 3.3       | 3.0       | 2.7       | 2.6       | 2.4       | 2.3       |
|            | 9q1   | 1.1       | 1.0       | 1.0       | 1.0       | 0.9       | 0.9       | 0.9       |
|            | 10q10 | 2.1       | 2.1       | 2.2       | 2.3       | 2.3       | 2.2       | 2.3       |
|            | 15q20 | 9.9       | 10.3      | 10.7      | 11.2      | 11.1      | 11.1      | 10.9      |
|            | 30q35 | 135.0     | 128.4     | 124.4     | 122.0     | 119.6     | 117.2     | 114.7     |
|            | 20q65 | 530.7     | 510.0     | 480.4     | 460.6     | 440.9     | 421.2     | 401.5     |
| Scenario 2 | 1q0   | 4.5       | 6.3       | 7.6       | 7.4       | 7.3       | 7.2       | 7.0       |
|            | 9q1   | 1.2       | 1.3       | 1.5       | 1.6       | 1.5       | 1.4       | 1.4       |
|            | 10q10 | 2.1       | 2.0       | 2.1       | 2.1       | 2.0       | 2.0       | 2.0       |
|            | 15q20 | 10.0      | 10.5      | 10.9      | 11.0      | 11.1      | 11.0      | 11.3      |
|            | 30q35 | 139.7     | 142.6     | 149.2     | 157.0     | 166.6     | 171.6     | 174.1     |
|            | 20q65 | 535.1     | 534.9     | 535.0     | 535.7     | 536.2     | 536.4     | 536.7     |
| Scenario 3 | 1q0   | 5.9       | 7.8       | 8.3       | 8.3       | 8.2       | 8.2       | 8.2       |
|            | 9q1   | 1.6       | 1.8       | 1.9       | 1.9       | 1.8       | 1.9       | 1.8       |
|            | 10q10 | 3.2       | 3.5       | 3.6       | 3.6       | 3.5       | 3.5       | 3.4       |
|            | 15q20 | 11.8      | 15.0      | 15.6      | 15.5      | 15.4      | 15.3      | 15.3      |
|            | 30q35 | 144.3     | 147.8     | 157.4     | 163.6     | 170.6     | 179.1     | 185.6     |
|            | 20q65 | 535.5     | 535.5     | 535.7     | 536.0     | 536.4     | 536.8     | 537.2     |

Source: own calculations

- Scenarios 2 and 3. Path 2. Extremely unfavourable. A progressive slow decrease in life expectancy and lower values in the end year (2050) compared to the start year (2014), especially for the younger and middle ages, and a slight increase for the older ones (over 65 years). In these scenarios, the probabilities of death in

childhood (<10 years) will increase sometime until 2030. Mortality in the ages 30-65 will also increase. A reversal of the declining trend occurs in the older ages (>65 years) in males. In females of the same age, mortality will not change much. For people aged 20-35 years, the mortality rates will either stabilize to low levels or increase firstly and stabilize later.

For further details on the methodology used to calculate these estimates, see Kotzamanis et al. (1026).

**Tab. 2: Probabilities of death forecasts by large age groups. Females.**

|            |       | 2015-2019 | 2020-2024 | 2025-2029 | 2030-2034 | 2035-2039 | 2040-2044 | 2045-2049 |
|------------|-------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Scenario 1 | 1q0   | 3.2       | 2.8       | 2.5       | 2.3       | 2.1       | 2.1       | 2.0       |
|            | 9q1   | 0.9       | 0.8       | 0.8       | 0.8       | 0.7       | 0.7       | 0.7       |
|            | 10q10 | 1.0       | 1.0       | 1.0       | 1.0       | 1.0       | 1.0       | 1.0       |
|            | 15q20 | 3.8       | 3.9       | 3.7       | 3.8       | 3.8       | 3.8       | 3.8       |
|            | 30q35 | 61.4      | 61.8      | 57.8      | 55.8      | 55.1      | 54.5      | 53.4      |
|            | 20q65 | 385.6     | 366.5     | 355.1     | 340.2     | 325.2     | 310.3     | 300.3     |
| Scenario 2 | 1q0   | 3.8       | 5.3       | 6.4       | 6.2       | 6.1       | 6.1       | 6.0       |
|            | 9q1   | 0.9       | 1.1       | 1.3       | 1.3       | 1.3       | 1.3       | 1.3       |
|            | 10q10 | 1.0       | 1.0       | 0.9       | 0.9       | 0.9       | 0.9       | 0.9       |
|            | 15q20 | 3.7       | 3.7       | 3.8       | 3.8       | 3.8       | 3.9       | 3.9       |
|            | 30q35 | 62.9      | 63.0      | 67.7      | 69.2      | 71.4      | 72.4      | 73.9      |
|            | 20q65 | 394.8     | 393.9     | 396.1     | 394.9     | 394.8     | 394.7     | 394.7     |
| Scenario 3 | 1q0   | 5.0       | 6.6       | 7.0       | 7.0       | 6.9       | 6.9       | 6.9       |
|            | 9q1   | 1.3       | 1.4       | 1.6       | 1.5       | 1.6       | 1.5       | 1.5       |
|            | 10q10 | 1.3       | 1.5       | 1.6       | 1.6       | 1.6       | 1.6       | 1.6       |
|            | 15q20 | 4.3       | 5.2       | 5.4       | 5.3       | 5.3       | 5.2       | 5.2       |
|            | 30q35 | 64.5      | 65.0      | 70.1      | 74.3      | 76.6      | 78.8      | 83.1      |
|            | 20q65 | 395.5     | 394.6     | 395.7     | 394.4     | 394.3     | 394.7     | 394.7     |

Source: own calculations

## 1.2 Calculation of full life tables

So far, only an estimation of the future trends of the probabilities of death in large age groups - except the first one took place:  $1q_0$ ,  $9q_1$ ,  $10q_{10}$ ,  $15q_{20}$ ,  $30q_{35}$  and  $20q_{65}$ . Note that the number on the left of the letter  $q$  denotes the size of an age group in years and the number on the right the first age at that group. Consequently, the question is how to expand these probabilities in one year-long age classes and construct a full life table afterwards. The entire procedure used, and its evaluation have been published by Zafeiris (2018).

This procedure begins with the relational method, developed by Kostaki (2000). According to this method, an abridged life table is expanded to a full one in relationship to another and known full life table, which is used as standard. The latter is denoted in the following formulas with the letter  $S$ . In an abridged life table, the one-year death probabilities  $q_{x+i}$  ( $i=0, 1, 2 \dots n-1$ ) in each of its  $n$  years intervals are equal to:

$$1 - \left(1 - q_{x+i}^{(S)}\right)^{nKx} \quad (1)$$

The term  $nKx$  equals to:

$$nKx = \frac{\ln(1-nqx)}{\sum_{i=0}^{n-1} \ln(1-q_{x+i}^{(S)})} \quad (2)$$

Thus, after calculating  $nKx$  using (2),  $q_{x+i}$  are calculated with (1). The following property must be fulfilled:

$$1 - \prod_{i=1}^{n-1} (1 - q_{x+i}) = nqx \quad (3)$$

The second step of this procedure is to smooth the one-year death probabilities curve. For this reason, a modified 9 parameters Heligman-Pollard formula was applied (see Heligman and Pollard, 1980; Kostaki, 1992).

$$\frac{q_x}{p_x} = \begin{cases} A^{(x+B)^C} + De^{-E_1(\ln x - \ln F)^2} + GH^x, & \text{for } x \leq F \\ A^{(x+B)^C} + De^{-E_3(\ln x - \ln F)^2} + GH^x, & \text{for } x > F \end{cases} \quad (4)$$

where, A, B, C, D, E<sub>1</sub>, E<sub>2</sub>, F, G, H are parameters that must be estimated by minimizing the term:

$$\sum_x \left(\frac{\widehat{q}_x}{q_x} - 1\right)^2 \quad (5)$$

where  $\widehat{q}_x$  is the fitted value for age  $x$  and  $q_x$  is the observed one. Before that, and because of the deviations of the ‘‘Heligman-Pollard’’ fitting process, three third order polynomials (see also <http://mathworld.wolfram.com/CubicSpline.html>) were used until the age of 84 years:

$$\widehat{q}_i = \widehat{q}_x + a_k(x_i - x) + b_k(x_i - x)^2 + c_k(x_i - x)^3 \quad (6)$$

The age-specific probabilities of death after the age of 84 years, were calculated by applying the last cubic spline of the fit. Finally, the life tables until the age of 110 years were calculated using conventional methods.

## 2 Calculation of Healthy Life Expectancy.

After calculating the  $q_x$  values, the age-specific mortality values ( $m_x$ ) were calculated by solving the well-known Chiang equation for  $m_x$ . Then, following Skiadas and Skiadas (2020), the Healthy Life Years Lost (HLYL) because of diseases and disabilities are coming from the following formula:

$$HLYL = \max \frac{xm_x}{\sum_0^x m_x} (7)$$

The healthy life expectancy at birth results from the subtraction of HLYL from Life expectancy at birth, calculated by the full life tables.

### 3 Results of the analysis.

Table 3 presents the results of the analysis. In scenario 1, the average longevity increases 3.4 years in males and 2.5 in females (Table 3). Consequently, the healthy life expectancy increases 3.3 and 2.6 years, respectively.

**Tab. 3: Life expectancy at birth (e0), Healthy Years Lost (HLYL), and Healthy Life expectancy (HLE).**

| Scenario | e0        | HLYL  | HLE   | e0        | HLYL  | HLE   | e0        | HLYL  | HLE   | e0        | HLYL  | HLE   |
|----------|-----------|-------|-------|-----------|-------|-------|-----------|-------|-------|-----------|-------|-------|
| Males    |           |       |       |           |       |       |           |       |       |           |       |       |
| 1        | 2014      |       |       | 2015-2019 |       |       | 2020-2024 |       |       | 2025-2029 |       |       |
|          | 78.42     | 10.67 | 67.75 | 78.76     | 10.50 | 68.26 | 79.33     | 10.56 | 68.77 | 79.96     | 10.60 | 69.36 |
|          | 2030-2034 |       |       | 2035-2039 |       |       | 2040-2044 |       |       | 2045-2049 |       |       |
|          | 80.38     | 10.62 | 69.76 | 80.84     | 10.65 | 70.19 | 81.31     | 10.67 | 70.64 | 81.79     | 10.70 | 71.09 |
| 2        | 2014      |       |       | 2015-2019 |       |       | 2020-2024 |       |       | 2025-2029 |       |       |
|          | 78.42     | 10.67 | 67.75 | 78.47     | 10.68 | 67.79 | 78.26     | 10.31 | 67.96 | 77.95     | 10.04 | 67.91 |
|          | 2030-2034 |       |       | 2035-2039 |       |       | 2040-2044 |       |       | 2045-2049 |       |       |
|          | 77.76     | 9.59  | 68.17 | 77.49     | 9.60  | 67.89 | 77.36     | 9.56  | 67.80 | 77.29     | 9.61  | 67.68 |
| 3        | 2014      |       |       | 2015-2019 |       |       | 2020-2024 |       |       | 2025-2029 |       |       |
|          | 78.42     | 10.67 | 67.75 | 78.02     | 10.71 | 67.31 | 77.63     | 10.20 | 67.43 | 77.32     | 9.58  | 67.75 |
|          | 2030-2034 |       |       | 2035-2039 |       |       | 2040-2044 |       |       | 2045-2049 |       |       |
|          | 77.16     | 9.56  | 67.60 | 76.96     | 9.55  | 67.41 | 76.70     | 9.53  | 67.17 | 76.52     | 9.52  | 67.00 |
| Females  |           |       |       |           |       |       |           |       |       |           |       |       |
| 1        | 2014      |       |       | 2015-2019 |       |       | 2020-2024 |       |       | 2025-2029 |       |       |
|          | 83.58     | 11.98 | 71.60 | 83.81     | 11.85 | 71.96 | 84.27     | 11.64 | 72.63 | 84.61     | 11.90 | 72.72 |
|          | 2030-2034 |       |       | 2035-2039 |       |       | 2040-2044 |       |       | 2045-2049 |       |       |
|          | 85.00     | 11.87 | 73.13 | 85.37     | 11.85 | 73.52 | 85.74     | 11.82 | 73.91 | 86.02     | 11.81 | 74.22 |
| 2        | 2014      |       |       | 2015-2019 |       |       | 2020-2024 |       |       | 2025-2029 |       |       |
|          | 83.58     | 11.98 | 71.60 | 83.54     | 11.90 | 71.64 | 83.41     | 11.86 | 71.55 | 83.18     | 11.60 | 71.58 |
|          | 2030-2034 |       |       | 2035-2039 |       |       | 2040-2044 |       |       | 2045-2049 |       |       |
|          | 83.12     | 11.81 | 71.32 | 83.07     | 11.76 | 71.31 | 83.07     | 11.64 | 71.43 | 83.04     | 11.63 | 71.41 |
| 3        | 2014      |       |       | 2015-2019 |       |       | 2020-2024 |       |       | 2025-2029 |       |       |
|          | 83.58     | 11.98 | 71.60 | 83.28     | 11.87 | 71.41 | 83.07     | 11.83 | 71.24 | 82.89     | 11.58 | 71.31 |
|          | 2030-2034 |       |       | 2035-2039 |       |       | 2040-2044 |       |       | 2045-2049 |       |       |
|          | 82.74     | 11.79 | 70.95 | 82.68     | 11.74 | 70.94 | 82.66     | 11.57 | 71.08 | 82.52     | 11.54 | 70.98 |

Source: own calculations

In the less favourable scenarios 2 and 3, the situation is quite different. The unfavourable conditions that are supposed to prevail in Greece will reduce the average longevity by the end of the projection period by 1.13 years according to scenario 2 and 1.9 according to scenario 3. However, the differential mortality developments in the large age groups will not seriously

disturb the healthy life expectancy in scenario 2. On the contrary, they will decrease it by one year in scenario 3.

In females, a similar situation persists. The average longevity is expected to decrease marginally by about 0.5 years following scenario 2, and almost one if scenario 3 will be confirmed. The decrease of healthy life expectancy will be marginal according to scenario 2 and half a year according to scenario 3.

Therefore, the average longevity during the projections period will change significantly in males and in a more moderate way in females, where the changes in health life expectancy are expected to be smaller. However, one must note once again that these results come after the formulation of mortality forecasts scenarios. Such scenarios could be either different or may cover a wide range of time. Thus, the estimations of future healthy life expectancy may vary a lot.

## **Conclusion**

In this paper, a presentation of the application of a direct method for calculating healthy life expectancy took place. After several elaborations, modifications and simplifications, this method (initially originated from the stochastic analysis) allows the direct estimation of the Healthy Life Years Lost in a population from life table data. Thus, it does not require any knowledge of the prevalence of diseases and disabilities, like the others described in the introductory section of this paper. Moreover, it can be used not only in contemporary populations but also in historical ones. One further application is its applicability and efficiency using mortality forecast data.

Such an application was demonstrated in this paper, presenting the expected levels of healthy life expectancy in the future of the population of Greece. By taking into consideration that data come from a research project which was completed several years ago, and considering the different scenarios, small but significant changes are expected to occur in the population of Greece in the future.

However, one must note that the quality of the findings of this direct method depends on the effectiveness of the projection and the time range it covers. Therefore, when this method is applied on mortality forecast data, quite expectedly, each result will depend on the quality, or the assumptions made for acquiring that data.

## **References**

- Chiang, C. L. (1965). *An Index of Health: Mathematical Models*, U.S. Department of HEW, Public Health Service, Publication No. ICXK. Series 2, No. 5.
- EUROSTAT. (n.d.). *Healthy Life Years Expectancy disability-free life expectancy – DFLE*. Method Retrieved September 16, 2020, available at: [https://ec.europa.eu/eurostat/cache/metadata/Annexes/hlth\\_hlye\\_esms\\_an1.pdf](https://ec.europa.eu/eurostat/cache/metadata/Annexes/hlth_hlye_esms_an1.pdf)
- Heligman, L., and Pollard, J. H. (1980). The age pattern of mortality. *Journal of the Institute of Actuaries*, 107, 47-80.
- Janssen, J. and Skiadas, C. H. (1995). Dynamic modelling of life table data. *Applied Stochastic Models and Data Analysis*, 11(1), 35-49.
- Kostaki, A. (2000) Relational Technique for estimating the age - specific mortality pattern from grouped data, *Mathematical Population Studies* 9(1), 83-95.
- Kostaki. (1992). A nine parameter version of the Heligman-Pollard formula. *Mathematical Population Studies*, 3(4), 277-288.
- Kotzamanis, B., Kostaki, A., Bergouignan, C., Zafeiris, K. N. and Mpaltas, P. (2016). The development of the population of Greece (2015-2050). DIANEOSIS. Athens. [In Greek]. <https://www.dianeosis.org/research/demography/>
- Sanders, B. S. (1964). Measuring Community Health Levels. *American Journal of Public Health* 54, 1063-1070. <https://doi.org/10.1002/asm.3150110106>
- Skiadas C.H. and Skiadas C. (2020). Relation of the Weibull Shape Parameter with the Healthy Life Years Lost Estimates: Analytical Derivation and Estimation from an Extended Life Table. In: Skiadas C.H., Skiadas C. (eds) *Demography of Population Health, Aging and Health Expenditures*. The Springer Series on Demographic Methods and Population Analysis, vol 50. Springer, Cham. [https://doi.org/10.1007/978-3-030-44695-6\\_2](https://doi.org/10.1007/978-3-030-44695-6_2)
- Sullivan, D. F. (1966). *Conceptual Problems in Developing an Index of Health*, U.S. Department of HEW, Public Health Service Publication No. 1000, Series 2, No. 17.
- Sullivan, D. F. (1971). A single index of mortality and morbidity. *HSMHA Health Reports*, 86, 347-354.
- Vos, T. et al. (2017). Global, regional, and national incidence, prevalence, and years lived with disability for 328 diseases and injuries for 195 countries, 1990–2016: a systematic analysis for the Global Burden of Disease Study 2016. *The Lancet*, 390 (10100), 1211–1259.
- WHO (1948). Preamble to the Constitution of the World Health Organization as adopted by the International Health Conference, New York, 19-22 June, 1946; signed on July 22 1946



by the representatives of 61 States (*Official Records of the World Health Organization*, no. 2, p. 100) and entered into force on April 7 1948.

Zafeiris, K. N. (2018). A method for the forecasting of mortality. In: C. Skiadas and Ch. Skiadas (eds.) *Demography and Health Issues: Mortality, Population Aging and Data Analysis*. The Springer Series on Demographic Methods and Population Analysis 46. Cham: Springer Verlag, pp. 71-82.

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